## **Curriculum Vitae**

### **Personal Information**

Family name: Velichkov First name: Bozhidar Web page: www.velichkov.it

Date of birth: 3 Feb 1985 e-mail: bozhidar.velichkov@unipi.it

#### Positions and cursus

Since 1 June 2020 I am Full Professor (Professore Ordinario) at Università di Pisa (Italy).

2019 - 2020. I was Associate Professor (Professore Associato) at

Università degli Studi di Napoli Federico II (Naples, Italy).

2014 – 2019. I was Assistant Professor (Maître de Conférences) at

Laboratoire Jean Kuntzmann - Université Grenoble Alpes (Grenoble, France).

2014 – 2014. I spent six months as Post-doc in Shape Optimization at Università di Pisa.

**2010 – 2013**. PhD at Scuola Normale Superiore and, since 2012, also at Université de Savoie with advisors Giuseppe Buttazzo and Dorin Bucur; discussion: 8 Nov 2013 in Pisa; mention: 70/70 cum Laude.

**2005 – 2010**. I was *Student in Mathematics* at SNS and I graduated with 70/70 cum Laude in 2010; as every SNS student, I was also a student at the University of Pisa:

- 2008 2010. Master in Mathematics Università di Pisa (110/110 cum Laude);
- 2005 2008. Bachelor in Mathematics Università di Pisa (110/110 cum Laude).

### **Honors and awards**

**2024.** Fubini Prize 2024.

2020. Book Prize UMI for my book "Regularity of the one-phase free boundaries" (Springer, 2023).

2019. ERC Starting Grant VAREG

**2013.** My PhD Thesis "Existence and Regularity Result for Some Shape Optimization Problems" was selected for publication in Edizioni della Normale (Springer, 2015).

## PhD students

Nuno Carneiro (since 2025; Università di Pisa, FCT);

Maria Antonietta Palladino (since 2024; Scuola Normale Superiore);

Federico Lai (since 2024; Università di Pisa);

Filippo Paiano (since 2023; Università di Pisa);

Matteo Carducci (since 2023; Scuola Normale Superiore);

Lorenzo Ferreri (since 2022; Scuola Normale Superiore);

François Générau (2017-2020; Université Grenoble Alpes); co-supervised with Edouard Oudet;

Baptiste Trey (2016-2020; Université Grenoble Alpes); co-supervised with Emmanuel Russ.

### **Post-docs**

Giulia Bevilacqua (1 Sept 2022 – );

Carlo Gasparetto (1 April 2023 – 30 April 2025);

Luca Benatti (1 Feb 2023 – 31 Jan 2024; co-supervised with Alessandra Pluda);

Roberto Ognibene (1 Feb 2022 – 31 March 2025);

Joseph Feneuil (1 Sept 2021 – 9 July 2022);

Giorgio Tortone (1 March 2021 – 28 Feb 2025).

### **Selected results**

## Logarithmic epiperimetric inequalities for the obstacle and the thin-obstacle problems

[CSV1] M. Colombo, L. Spolaor, B. Velichkov. *A logarithmic epiperimetric inequality for the obstacle problem.* Geom. Funct. Anal. 28 (4) (2018), 1029–1061.

[CSV2] M. Colombo, L. Spolaor, B. Velichkov. *Direct epiperimetric inequalities for the thin obstacle problem and applications*. Comm. Pure. Appl. Math. 73 (2) (2020), 384–420.

## Regularity theory for one-phase free boundary problems

[FTV] L. Ferreri, G. Tortone, B. Velichkov. *A capillarity one-phase Bernoulli free boundary problem*. Preprint ArXiv (2023).

[FV] L. Ferreri, B. Velichkov. *Regularity for one-phase Bernoulli problems with discontinuous weights and applications.* Trans. Amer. Math. Soc. (2024), to appear.

[ESV] M. Engelstein, L. Spolaor, B. Velichkov. *Uniqueness of the blow-up at isolated singularities for the Alt-Caffarelli functional.* **Duke Math. J.** 169 (8) (2020), 1541–1601.

## Regularity theory for two-phase free boundary problems

[SV] L. Spolaor, B. Velichkov. An epiperimetric inequality for the regularity of some free boundary problems: the 2-dimensional case. Comm. Pure. Appl. Math. 72 (2) (2018), 375–421.

[DSV1] G. De Philippis, L. Spolaor, B. Velichkov. *Regularity of the free boundary for the two-phase Bernoulli problem.* Invent. Math. 225 (2021), 347–394.

[DSV2] G. De Philippis, L. Spolaor, B. Velichkov. (*Quasi-)conformal methods in two-dimensional free boundary problems.* J. Eur. Math. Soc. (2024), doi: 10.4171/JEMS/1435

# Regularity theory for vectorial Bernoulli problems and free boundary systems

[MTV1] D. Mazzoleni, S. Terracini, B. Velichkov. *Regularity of the optimal sets for some spectral functionals.* Geom. Funct. Anal. 27 (2017), 373–426.

[MTV2] D. Mazzoleni, S. Terracini, B. Velichkov. *Regularity of the free boundary for the vectorial Bernoulli problem.* Anal. PDE 13 (3) (2020), 741–764.

[MTV3] F. Maiale, G. Tortone, B. Velichkov. *Epsilon-regularity for the solutions of a free boundary system.* Rev. Mat. Iberoam. 39 (5) (2023), 1947–1972.

### **Regularity of optimal shapes**

[BMMTV] G.Buttazzo, F. Maiale, D. Mazzoleni, G. Tortone, B. Velichkov. *Regularity of the optimal sets for a class of integral shape functionals.* Arch. Rat. Mech. Anal. (2024), to appear.

[MTV4] D. Mazzoleni, B. Trey, B. Velichkov. *Regularity of the optimal sets for the second Dirichlet eigenvalue*. Ann. Inst. H. Poincaré Anal. Non Linéaire 39 (3) (2022), 529–573.

[RTV] E. Russ, B. Trey, B. Velichkov. *Existence and regularity of optimal shapes for elliptic operators with drift.* Calc. Var. PDE 58 (2019).

[BMPV] D. Bucur, D. Mazzoleni, A. Pratelli, B. Velichkov. *Lipschitz regularity of the eigenfunctions on optimal domains*. **Arch. Rat. Mech. Anal.** 216 (2015), 117–151.

# Regularity theory for optimal partition problems

[OV2] R. Ognibene, B. Velichkov. Structure of the free interfaces near triple junction singularities in harmonic maps and optimal partition problems. Preprint ArXiv (2024).

[OV1] R. Ognibene, B. Velichkov. Boundary regularity of the free interface in spectral optimal partition problems. Preprint ArXiv (2024).

## Free boundary minimal surfaces

[BSV] G. Bevilacqua, S. Stuvard, B. Velichkov. Classical solutions to the soap film capillarity problem for plane boundaries. **Math. Ann.** 392 (2025), 4607–4659.

#### Mini courses

- "Free boundary regularity for the one-phase Bernoulli problem" (6 hours). Summer school "Free boundary problems and related topics" (ETH Zürich, 2022).
- "Regularity of the one-phase free boundaries" (6 hours). Summer school "Shape optimization, control and inverse problems for PDEs" (Naples, 2019).

### Selected talks

- "Regularity up to the boundary for optimal partition problems" Workshop Calculus of Variations (Oberwolfach, 2024).
- "On the fine structure of the two-phase free boundaries" Workshop Partial Differentials Equations (Oberwolfach, 2023).
- "Free boundary clusters with two phases" MSRI Workshop "Regularity Theory for Minimal Surfaces and Mean Curvature Flow" online (22/3/2022).
- "An epsilon-regularity theorem for the solutions of a vectorial free boundary system" Workshop Partial Differentials Equations (Oberwolfach, 2021).
- "Vectorial free boundary problems and regularity of the optimal sets for the eigenvalues of the Dirichlet Laplacian". One world PDE Seminar online (2/3/2021).
- "Regularity of the two-phase free boundaries." Workshop Calculus of Variations (Oberwolfach, 2020).
- "Regularity of the two-phase free boundaries." XXX Convegno Nazionale di Calcolo delle Variazioni (Levico Terme, 2020).
- "On the logarithmic epiperimetric inequality." Partial Differentials Equations (Oberwolfach, 2019).
- "On the logarithmic epiperimetric inequality." XXIX Convegno Nazionale di Calcolo delle Variazioni (Levico Terme, 2019).
- Approche variationnelle à la régularité des frontières libres singulières. Laboratoire Jacques-Louis Lions (05/02/2018).
- "Variational approach to the regularity of the singular free boundaries."
  Seminar at ETH Zürich, 13/03/2018.
- "Recent results on the regularity of the free boundary of the obstacle problem." Calculus of Variations at Paris-Diderot (Paris, 2018).
- "Regularity of the free boundaries around isolated singularities." Seminar at Université Paris Sud Orsay, 26/01/2018.
- "Regularity of the optimal sets for spectral functionals." Seminar at Max Planck Institut Leipzig, 13/05/2016.
- "Regularity of the optimal sets for spectral functionals." Seminar at Universität Zürich, 13/04/2016. Séminaire Parisien d'Optimisation, 6/10/2014.

### Organization of workshops and conferences

**Regularity Theory for Free Boundary and Geometric Variational Problems** – one week conferences; 21 speakers per event; 5 editions: 2021 (Levico), 2022 (Pisa), 2023 (Levico), 2024 (Levico), 2025 (Cervia); jointly organized with Giulia Bevilacqua, Roberto Ognibene, Luca Spolaor.

Calculus of Variations and Free Boundary Problems – one day workshops; two in 2025 (Pisa); three in 2024 (Pisa); two in 2023 (Pisa); one in 2022 (Pisa), 2019 (Napoli), 2018 (Grenoble), 2017 (Grenoble); a complete list can be found here: http://www.velichkov.it/events.html

## **Projects**

**PI of an ERC Starting Grant project (2020-2025).** PI of the project ERC Starting Grant "VAREG - Variational approach to the regularity of the free boundaries" (project number: 853404; duration: 66 months; volume 1,330 kE; starting date: 1 June 2020; host institution: Università di Pisa; web page: http://www.velichkov.it/vareg.html).

**Local Coordinator of a national PRIN project** (2023-2025). Local Coordinator (for Università di Pisa) of the project PRIN 2022 "NO<sup>3</sup> - Nodal Optimization, NOnlinear elliptic equations, NOnlocal geometric problems, with a focus on regularity" financed by MIUR (volume 200kE; duration: 24 months; PI: Nicola Soave).

**PI of a project at University of Pisa** (2022-2024). PI of the project PRA "GeoDom - Geometric evolution problems and PDEs on variable domains" financed by the University of Pisa (duration: 24 months; volume 50 kE; web page: http://www.velichkov.it/geodom.html).

**Local Coordinator of a national ANR project (2018-2019).** Local Coordinator (for Laboratoire Jean Kuntzmann – Université Grenoble Alpes) of the project ANR "ShapO - Shape Optimization" financed by the French National Research Agency - ANR (duration: 48 months; starting date: 10/2018; volume 300 kE; PI: Jimmy Lamboley).

PI of a project at Université Grenoble Alpes (2015-2016). PI of "VariForm - Méthodes Variation-nelles en Optimisation de Formes" (Université Grenoble Alpes, 24 months, 15 kE).

**Participation to other national projects.** Member of the projects ANR "Geospec - Geometry and Spectral Optimization" (2016-2020) and ANR "CoMeDiC - Convergent Metrics for Digital Calculus" (2015-2020) financed by the French National Research Agency - ANR.

### **Selection committees and administration**

# PhD school in Mathematics (University of Pisa).

Since 11/2022 I am deputy coordinator of the PhD school in Mathematics at the Department of Mathematics, University of Pisa, appointed by the coordinator Roberto Frigerio.

In 2025 I was member (with Cecilia Pagliantini and Michele D'Adderio) of the selection committee for the entrance exam of the PhD school in Mathematics for the academic year 2025/2026.

In 2024 I was member (with Carlo Petronio and Cecilia Pagliantini) of the selection committee for the entrance exam of the PhD school in Mathematics for the academic year 2024/2025.

## Selection committees at Scuola Normale Superiore.

In Sept 2020 and Sept 2022 I was member of the evaluation committees for the entrance exams (for the 1st and 4th years) at Scuola Normale Superiore respectively for the academic years 2020/2021 (chair: Franco Flandoli) and 2022/2023 (chair: Angelo Vistoli).

#### Referee of PhD thesis.

- **2024.** Federico Franceschini (ETH Zürich; advisors: Alessio Figalli and Joaquim Serra);
- **2024.** Clara Torres Latorre (Universitat de Barcelona; advisor: Xavier Ros-Oton);
- **2018.** Harish Shrivastava (Università di Pisa; advisor: Giuseppe Buttazzo);

### **Selection committees for permanent positions.**

- **2022.** Call for Associate Professor (Professore Associato) at Università di Torino.
- **2021.** Call for Full Professor (Professore Ordinario) at Università di Pisa.
- **2021.** Call for a Tenure-Track (RTDB) position at Università di Torino.