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## Curriculum Vitae

### Personal Information

Family name: Velichkov      First name: Bozhidar      Web page: [www.velichkov.it](http://www.velichkov.it)  
Date of birth: 03 Feb 1985      e-mail: [bozhidar.velichkov@unipi.it](mailto:bozhidar.velichkov@unipi.it)

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### Positions and cursus

**Since 1 June 2020.** I am Full Professor (Professore Ordinario) at  
Università di Pisa (Pisa, Italy)

**2019 – 2020.** I was Associate Professor (Professore Associato) at  
Università degli Studi di Napoli Federico II (Naples, Italy).

**2014 – 2019.** I was Assistant Professor (Maître de Conférences) at  
Laboratoire Jean Kuntzmann - Université Grenoble Alpes (Grenoble, France).

**2014 – 2014.** I spent six months as Post-doc in Shape Optimization at Università di Pisa .

**2010 – 2013.** I was PhD student (Perfezionando) at *Scuola Normale Superiore SNS*, and, since 2012, also at *Laboratoire de Mathématiques LAMA - Université de Savoie*; I discussed on 8 Nov 2013 in Pisa; mention: 70/70 cum Laude; advisors: Giuseppe Buttazzo and Dorin Bucur.

**2005 – 2010.** I was *Student in Mathematics* at SNS and I graduated with 70/70 cum Laude in 2010; as every SNS student, I was also a student at the University of Pisa:

- 2008 – 2010. Master in Mathematics - Università di Pisa (110/110 cum Laude);
  - 2005 – 2008. Bachelor in Mathematics - Università di Pisa (110/110 cum Laude).
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### Honors and awards

**2020.** *Book Prize UMI* for the lecture notes *Regularity of the one-phase free boundaries*.

**2019.** P.I. of the project *ERC Starting Grant VAREG*

**2015.** PEDR - *Prime d'Encadrement Doctoral et de Recherche*

**2013.** My PhD Thesis "*Existence and Regularity Result for Some Shape Optimization Problems*" was selected for publication in *Edizioni della Normale* (n.19, Springer 2015, ISBN 978-88-7642-526-4).

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### PhD students

Filippo Paiano (since 2023; Università di Pisa);

Matteo Carducci (since 2023; Scuola Normale Superiore);

Lorenzo Ferreri (since 2022; Scuola Normale Superiore);

François Générault (2017-2020; Université Grenoble Alpes); co-supervised with Edouard Oudet;

Baptiste Trey (2016-2020; Université Grenoble Alpes); co-supervised with Emmanuel Russ.

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### Post-docs

Carlo Gasparetto (1 April 2023 - );

Luca Benatti (1 Feb 2023 – 31 Jan 2024; co-supervised with Alessandra Pluda);

Giulia Bevilacqua (1 Sept 2022 - );

Roberto Ognibene (1 Feb 2022 - );

Joseph Feneuil (1 Sept 2021 – 9 July 2022);

Giorgio Tortone (1 March 2021 - ).

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**Selected results**
**Logarithmic epiperimetric inequalities for the obstacle and the thin-obstacle problems.**

[CSV1] M. Colombo, L. Spolaor, B. Velichkov. *A logarithmic epiperimetric inequality for the obstacle problem*. **Geom. Funct. Anal.** 28 (4) (2018), 1029–1061.

[CSV2] M. Colombo, L. Spolaor, B. Velichkov. *Direct epiperimetric inequalities for the thin obstacle problem and applications*. **Comm. Pure. Appl. Math.** 73 (2) (2020), 384–420.

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**Regularity theory for two-phase free boundary problems.**

[SV] L. Spolaor, B. Velichkov. *An epiperimetric inequality for the regularity of some free boundary problems: the 2-dimensional case*. **Comm. Pure. Appl. Math.** 72 (2) (2018), 375–421.

[DSV1] G. De Philippis, L. Spolaor, B. Velichkov. *Regularity of the free boundary for the two-phase Bernoulli problem*. **Invent. Math.** 225 (2021), 347–394.

[DSV2] G. De Philippis, L. Spolaor, B. Velichkov. *(Quasi-)conformal methods in two-dimensional free boundary problems*. **J. Eur. Math. Soc.** (2024), doi: 10.4171/JEMS/1435

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**Regularity theory for vectorial Bernoulli problems and free boundary systems.**

[MTV1] D. Mazzoleni, S. Terracini, B. Velichkov. *Regularity of the optimal sets for some spectral functionals*. **Geom. Funct. Anal.** 27 (2017), 373–426.

[MTV2] D. Mazzoleni, S. Terracini, B. Velichkov. *Regularity of the free boundary for the vectorial Bernoulli problem*. **Anal. PDE** 13 (3) (2020), 741–764.

[MTV3] F. Maiale, G. Tortone, B. Velichkov. *Epsilon-regularity for the solutions of a free boundary system*. **Rev. Mat. Iberoam.** 39 (5) (2023), 1947–1972.

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**Regularity theory for one-phase free boundary problems.**

[FTV] L. Ferreri, G. Tortone, B. Velichkov. *A capillarity one-phase Bernoulli free boundary problem*. **Preprint ArXiv** (2023).

[FV] L. Ferreri, B. Velichkov. *Regularity for one-phase Bernoulli problems with discontinuous weights and applications*. **Trans. Amer. Math. Soc.** (2024), to appear.

[book] B. Velichkov. *Regularity of the one-phase free boundaries*. Lecture notes of the Unione Matematica Italiana, Springer (2023).

[ESV] M. Engelstein, L. Spolaor, B. Velichkov. *Uniqueness of the blow-up at isolated singularities for the Alt-Caffarelli functional*. **Duke Math. J.** 169 (8) (2020), 1541–1601.

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**Regularity of optimal shapes.**

[BMMTV] G. Buttazzo, F. Maiale, D. Mazzoleni, G. Tortone, B. Velichkov. *Regularity of the optimal sets for a class of integral shape functionals*. **Arch. Rat. Mech. Anal.** 248 (2024), to appear.

[MTV4] D. Mazzoleni, B. Trey, B. Velichkov. *Regularity of the optimal sets for the second Dirichlet eigenvalue*. **Ann. Inst. H. Poincaré Anal. Non Linéaire** 39 (3) (2022), 529–573.

[RTV] E. Russ, B. Trey, B. Velichkov. *Existence and regularity of optimal shapes for elliptic operators with drift*. **Calc. Var. PDE** 58, 199 (2019).

[BMPV] D. Bucur, D. Mazzoleni, A. Pratelli, B. Velichkov. *Lipschitz regularity of the eigenfunctions on optimal domains*. **Arch. Rat. Mech. Anal.** 216 (2015), 117–151.

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**Regularity theory for optimal partition problems.**

[OV] R. Ognibene, B. Velichkov. *Boundary regularity of the free interface in spectral optimal partition problems*. **Preprint ArXiv** (2024).

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### Mini courses

- "Free boundary regularity for the one-phase Bernoulli problem" (6 hours).  
Summer school "Free boundary problems and related topics" (ETH Zürich, 2022).
- "Regularity of the one-phase free boundaries" (6 hours).  
Summer school "Shape optimization, control and inverse problems for PDEs" (Naples, 2019).

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### Selected talks

- "On the fine structure of the two-phase free boundaries".  
Workshop Partial Differential Equations (Oberwolfach, 2023).
- "Free boundary clusters with two phases". MSRI Workshop "Regularity Theory for Minimal Surfaces and Mean Curvature Flow" - online (22/3/2022).
- "An epsilon-regularity theorem for the solutions of a vectorial free boundary system".  
Workshop Partial Differential Equations (Oberwolfach, 2021).
- "Vectorial free boundary problems and regularity of the optimal sets for the eigenvalues of the Dirichlet Laplacian". One world PDE Seminar - online (2/3/2021).
- "Regularity of the two-phase free boundaries".  
Workshop Calculus of Variations (Oberwolfach, 2020).
- "Regularity of the two-phase free boundaries".  
XXX Convegno Nazionale di Calcolo delle Variazioni (Levico Terme, 2020).
- "On the logarithmic epiperimetric inequality".  
Partial Differential Equations (Oberwolfach, 2019).
- "On the logarithmic epiperimetric inequality".  
XXIX Convegno Nazionale di Calcolo delle Variazioni (Levico Terme, 2019).
- "Approche variationnelle à la régularité des frontières libres singulières".  
Laboratoire Jacques-Louis Lions (05/02/2018).
- "Variational approach to the regularity of the singular free boundaries."  
Seminar at ETH Zürich, 13/03/2018.
- "Recent results on the regularity of the free boundary of the obstacle problem".  
Calculus of Variations at Paris-Diderot (Paris, 2018).
- "Regularity of the free boundaries around isolated singularities".  
Seminar at Université Paris Sud - Orsay, 26/01/2018.
- "Regularity of the optimal sets for spectral functionals".  
Seminar at Max Planck Institut Leipzig, 13/05/2016.
- "Regularity of the optimal sets for spectral functionals".  
Seminar at Universität Zürich, 13/04/2016.

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### Organization of workshops and conferences

**Regularity Theory for Free Boundary and Geometric Variational Problems** – one week conferences; 21 speakers per event; 4 editions: 2021 (Levico), 2022 (Pisa), 2023 (Levico), 2024 (Levico); jointly organized with Luca Spolaor.

**Calculus of Variations and Free Boundary Problems** – one day workshops; 4-5 speakers; 8 editions: two in 2024 (Pisa); two in 2023 (Pisa); one in 2022 (Pisa), 2019 (Napoli); 2018 (Grenoble); 2017 (Grenoble); a complete list can be found here: <http://www.velichkov.it/events.html>

## Projects

**PI of an ERC Starting Grant project (2020-2025).** I am PI of the project ERC Starting Grant "VAREG - Variational approach to the regularity of the free boundaries" (project number: 853404; duration: 66 months; volume 1,330 kE; starting date: 1 June 2020; host institution: Università di Pisa; web page: <http://www.velichkov.it/vareg.html>).

**Local Coordinator and Deputy PI of a national PRIN project (2023-2025).** I am Deputy PI and Local Coordinator (for Università di Pisa) of the project PRIN 2022 "NO<sup>3</sup> - Nodal Optimization, NONlinear elliptic equations, NONlocal geometric problems, with a focus on regularity" financed by MIUR (volume 200kE; duration: 24 months; PI: Nicola Soave).

**PI of a local project at University of Pisa (2022-2024).** I am PI of the project PRA "GeoDom - Geometric evolution problems and PDEs on variable domains" financed by the University of Pisa (duration: 24 months; volume 50 kE; web page: <http://www.velichkov.it/geodom.html>).

**Local Coordinator of a national ANR project (2018-2019).** I was Local Coordinator (for Laboratoire Jean Kuntmann – Université Grenoble Alpes) of the project ANR "ShapO - Shape Optimization" financed by the French National Research Agency - ANR (duration: 48 months; starting date: 10/2018; volume 300 kE; PI: Jimmy Lamboley).

**PI of a local project at Université Grenoble Alpes (2015-2016).** I was PI of the project "Vari-Form - Méthodes Variationnelles en Optimisation de Formes" financed by Université Grenoble Alpes (duration: 24 months; volume 15 kE).

**Participation to other national projects.** I was member of the projects ANR "Geospec - Geometry and Spectral Optimization" (2016-2020) and ANR "CoMeDiC - Convergent Metrics for Digital Calculus" (2015-2020) financed by the French National Research Agency - ANR.

## Selection committees and administration

### PhD school in Mathematics (University of Pisa).

Since 11/2022 I am deputy coordinator of the PhD school in Mathematics at the Department of Mathematics, University of Pisa, appointed by the coordinator Roberto Frigerio.

In 2024 I was member (with Carlo Petronio and Cecilia Pagliantini) of the selection committee for the entrance exam of the PhD school in Mathematics for the academic year 2024/2025.

### Selection committees at Scuola Normale Superiore.

In Sept 2020 and Sept 2022 I was member of the evaluation committees for the entrance exams (for the 1st and 4th years) at Scuola Normale Superiore respectively for the academic years 2020/2021 (chair: Franco Flandoli) and 2022/2023 (chair: Angelo Vistoli).

### Referee of PhD thesis.

**2024.** Federico Franceschini (ETH Zürich; advisors: Alessio Figalli and Joaquim Serra);

**2024.** Clara Torres Latorre (Universitat de Barcelona; advisor: Xavier Ros-Oton);

**2018.** Harish Shrivastava (Università di Pisa; advisor: Giuseppe Buttazzo).

### Participation to selection committees for permanent positions.

**2022.** Call for Associate Professor (Professore Associato) at Università di Torino.

**2021.** Call for Full Professor (Professore Ordinario) at Università di Pisa.

**2021.** Call for a Tenure-Track (RTDB) position at Università di Torino.